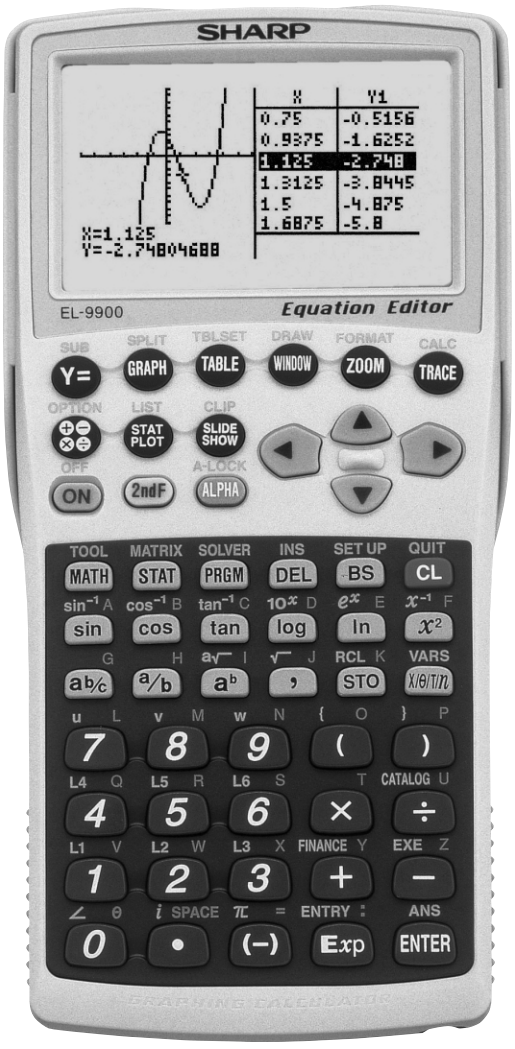
SHARP

Graphing Calculator

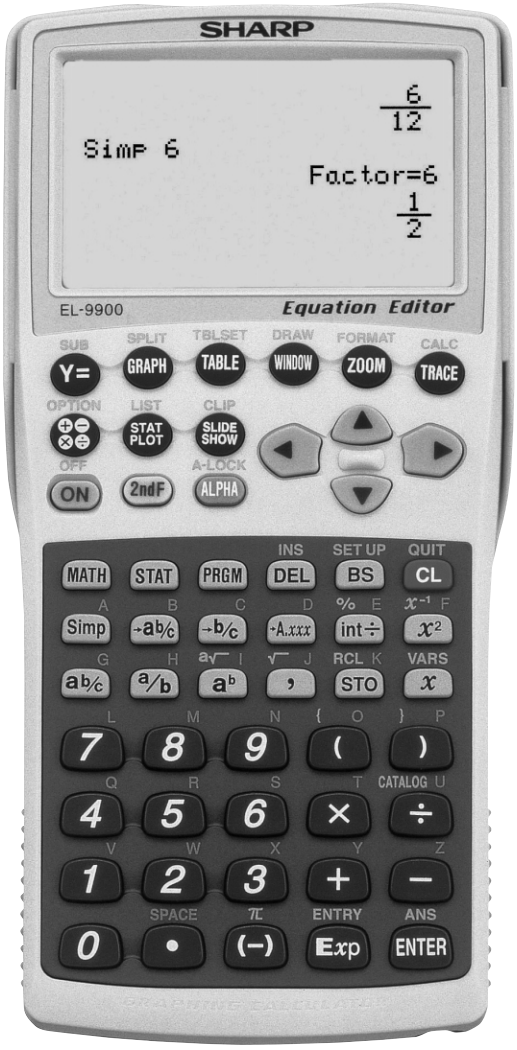
# EL-9900

# Handbook Vol. 2

## Programmes




For Advanced Levels




For Basic Levels

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# Read this first

This handbook was produced for practical application of the SHARP EL-9900 Graphing Calculator. This calculator includes a highly convenient programming function, which enables automatic processing of both simple and complex calculations any number of times.

## 1. Entering and Editing a Programme (Advanced keyboard mode only):

Programmes can be entered and edited either by pressing the calculator keys or by downloading from a PC. To download programmes from a PC, you will need the CE-LK2 PC link software (sold separately).

In this handbook, we use the symbol "∗" to represent multiplication, and the symbol "/" to represent division. Please follow this convention when entering and editing programmes via the PC-Link software. When entering programmes directly through the EL-9900's keypad, meanwhile, please use the [X] and [÷] keys.

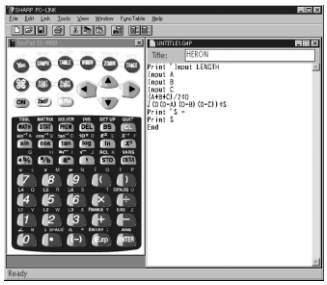
### A. Using calculator keys

- Creating a new programme:
  1. Press [PRGM] to display the programme menu.
  2. Press [C] [ENTER] to select the new programme menu. (See right)
  3. Enter the programme title, then press [ENTER].
  4. Enter the programme.
  5. Press [2nd F] [QUIT] to finish programming.

- Editing a programme:
  1. Press [PRGM] to display the programme menu.
  2. Press [B] and choose the number of the programme you wish to edit.
  3. Press [2nd F] [QUIT] to finish editing. (See right)

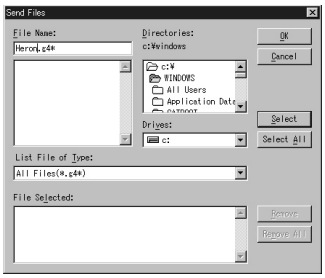
### B. Downloading from PC

- Creating a new programme:
  1. Using the CE-LK2, select **New** from the **File** menu.
  2. Enter a programme name in **Title:**.
  3. Enter a programme. (For details on entering a programme, refer to the operation manual.) (See right)



- Programmes can also be downloaded from Sharp's website at http://sharp-world.com/products/calculator/education/program/index.html instead of creating a new programme.

- Sending programmes from a PC:
  1. Using the CE-LK2, select the **Communication Port** from the **Link** menu and click on the port to be used.
  2. Turn off the EL-9900 and connect it to the PC.
  3. Turn on the EL-9900
  4. Select **Send…** from the **Link** menu of the CE-LK2 (See right)
  5. Specify the kind of drive, folder, and file, then select the file to be sent from the file list, and click on the **Select** button.
  6. Click on the **OK** button.




*Note :* For further details refer to the manual.

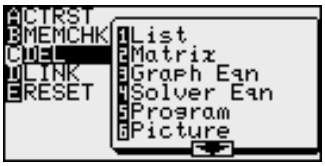
## 2. Executing a programme:

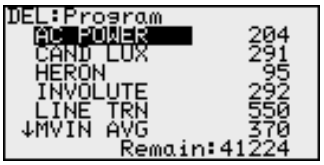
1. Press [PRGM] to display the execute menu.
2. Press [A] [ENTER] and choose the number of the programme you wish to execute. (See right)
3. Follow the instructions.

## 3. Deleting a programme:

Press [2nd F] [OPTION] [C] and then choose [5] to select the programme to be deleted.

*Note:* Do not try to erase a programme by resetting all memories to the initial condition as programme data to be stored will also be deleted. Also, it is advised to use the CE-LK2 PC link software to back up any programmes not to be erased.




## 4. Using the keys:

Press [2nd F] to use secondary functions (in yellow).
To select "$x^{-1}$": [2nd F] [$x^2$] → Displayed as follows: [2nd F] [$x^{-1}$]

Press [ALPHA] to use the alphabet keys (in violet).
To select F: [ALPHA] [$x^2$] → Displayed as follows: [ALPHA] [F]

Press [2nd F] [A-LOCK] to continue input of violet letters.
To input ABC: [ALPHA] [A] [ALPHA] [B] [ALPHA] [C] or [2nd F] [A-LOCK] [A] [B] [C]
(To return to the normal function, press [ALPHA] again.)

## 5. Troubleshooting:

Following is a list of error codes and error messages.

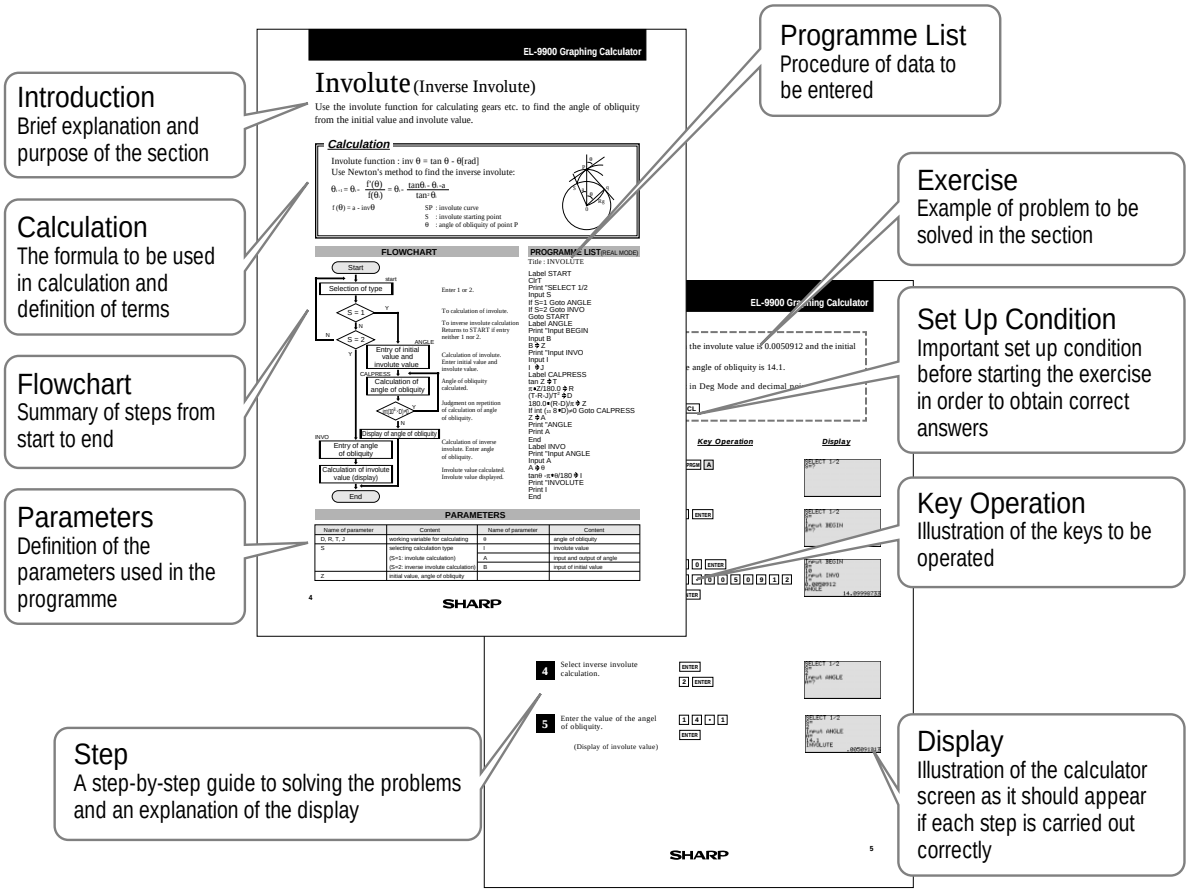
When errors occur, refer to pages 233 and 234 of the manual.

| Error code | Error message | Error content |
|---|---|---|
| 01 | Syntax | Syntax error found in equation/programme. |
| 02 | Calculate | Calculation-related error found (division by 0, calculation beyond range, etc.). |
| 03 | Nesting | Cannot nest more than 14 numerical values, or 32 functions during execution. |
| 04 | Invalid | Matrix definition error or entering an invalid value. |
| 05 | Dimension | Matrix dimension, or STAT list dimension, inconsistent. |
| 07 | Invalid DIM | Size of list/matrix exceeds calculation range. |
| 08 | Argument | Inconsistency found in argument of the structured function. |
| 09 | Data Type | Invalid data type used in calculation. |
| 10 | No Sign Change | Financial calculation error found. |
| 11 | No define | Undefined list/matrix used in calculation. |
| 12 | Domain | Argument definition outside of domain. |
| 13 | Increment | Increment error found. |
| 16 | Irr Calc | More than two inflection points for Irr calculation. |
| 17 | Stat Med | Med-Med law (statistic) error found. |
| 20 | No Argument | Argument missing. |
| 21 | Not pair ∫ dx | ∫ and dx are not used in a pair. |
| 22 | Not pair [ ] | Brackets are not used in a pair. |
| 23 | Not pair ( ) | Parentheses are not used in a pair. |
| 24 | Not pair { } | Braces are not used in a pair. |
| 25 | Line over | Line is over the capacity. |
| 26 | Not delete | Unable to delete a selected item. |
| 27 | Buffer over | Input/equation exceeds buffer capability. |
| 30 | Edit type | Invalid editor type found.* |
| 31 | Continue = | " = " exists in equation that has been recalled (RCL). |
| 32 | No data | Data does not exist. |
| 33 | Graph Type | Graph type setting incorrect. |
| 34 | Too many var. | Too many variables assigned in the SOLVER. |
| 35 | No variable | No variable specified in the SOLVER. |
| 36 | No solution | No solution found. |
| 37 | No title | No title entered. |
| 38 | Too many obj | More than 30 objects selected. |

| Error code | Error message | Error content |
|---|---|---|
| 40 | Lbl duplicate | Labels with identical name found in programme. |
| 41 | Lbl undefined | Goto/Gosub encountered with no defined label. |
| 42 | Lbl over | More than 50 labels found in programme. |
| 43 | Gosub stack | Nesting of more than 10 subroutines found. |
| 44 | Line too long | Line contains more than 160 characters. |
| 45 | Can't return | Return used without jumping from subroutine. |
| 46 | Storage full | Cannot create more than 99 files. |
| 47 | Coord type | Invalid coordinate system for command. |
| 48 | Without For | For is missing corresponding to the Next command. |
| 49 | Without WEnd | WEnd is missing corresponding to the While command. |
| 50 | Without While | While is missing corresponding to the WEnd command. |
| 51 | Without Then | Then is missing corresponding to the If command. |
| 52 | Without EndIf | EndIf is missing corresponding to the If command. |
| 53 | Without If | If is missing corresponding to the EndIf command. |
| 70 | I/O device | Communication error found among devices. |
| 71 | Wrong Mode | Wrong communication mode set. |
| 90 | Memory over | Memory is full; cannot store data as requested. |
| 99 | System error | System error found; user memory space is insecure. |
| | Low battery | Operation interrupted due to low battery power. |
| | BREAK!! | Operation break specified. |

* The following operations may cause Editor type error. Correct the Editor type to continue.
  - Recall the SOLVER equations (EQTN) or Graph data (G_DATA) stored in a different EDITOR mode than currently in use.
  - Receive the Graph equation (Y1 and others) entered in a different EDITOR mode than currently in use.

# 6. Page Layout



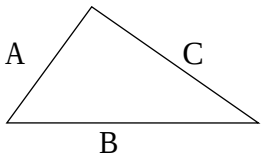
# Heron's Formula

Use Heron's formula to find the area of a triangle when the sides (A,B,C) of the triangle are known.

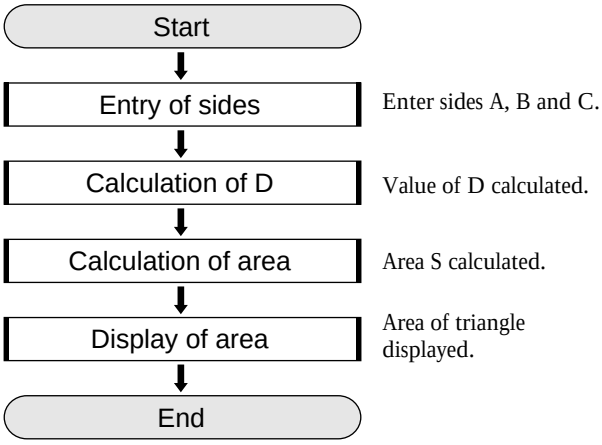
## *Calculation*

$$S = \sqrt{D\,(D - A)\,(D - B)\,(D - C)}$$

$$D = \frac{(A + B + C)}{2}$$




## FLOWCHART




## PROGRAMME LIST(REAL MODE)

Title : HERON

```
Print "Input LENGTH
Input A
Input B
Input C
(A+B+C)/2⇒D
√(D (D-A) (D-B) (D-C) )⇒S
Print "S =
Print S
End
```

## PARAMETERS

| Name of parameter | Content | Name of parameter | Content |
|---|---|---|---|
| A | value of side A | D | value of D |
| B | value of side B | S | area |
| C | value of side C | | |

## *Exercise*

Find the area of a triangle when sides A, B and C are 20, 35 and 40cm respectively.

| *Step* | | *Key Operation* | *Display* |
|---|---|---|---|
| **1** | Specify the programme mode.<br>Select the title HERON. | PRGM A | HERON<br>INPUT LENGTH<br>A=? |
| **2** | Enter the values A, B and C.<br><br>(Display of area) | 2 0 ENTER 3 5<br>ENTER 4 0 ENTER | A=<br>20<br>B=<br>35<br>C=<br>40<br>S=<br>349.944192 |
| **3** | The area is approximately 350cm$^2$. | | |

# Calculating Tension

Use the law of sines to find the tension when a pole of weight W is suspended with two strings, and the strings are balanced with the angles from the vertical line A and B.

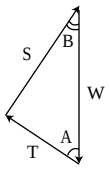
## *Calculation*

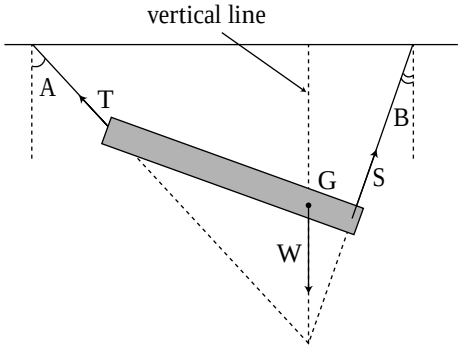
$$\frac{T}{\sin B} = \frac{S}{\sin A} = \frac{W}{\sin (A+B)}$$

$$\therefore T = W\frac{\sin B}{\sin (A+B)}$$

$$\therefore S = W\frac{\sin A}{\sin (A+B)}$$

T, S : tension  W : weight
A, B : angles (6 sexagesimal numbers)

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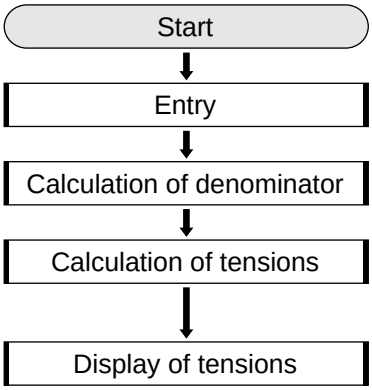



Enter angles and weight A, B and W.

Denominator in law of sines calculated. C= sin (A + B)

Tensions T and S calculated.
T = W ∗ sin B/C
T = W ∗ sin A/C

Tensions T and S displayed.

## PROGRAMME LIST(REAL MODE)

Title : TENSION

```
Print "Input ANGLE
Input A
Input B
Print "Input WEIGHT
Input W
sin (A+B)⇒C
W∗sin B/C⇒T
W∗sin A/C⇒S
Print "TENSION
Print "T=
Print T
Print "S=
Print S
End
```

## PARAMETERS

| Name of parameter | Content | Name of parameter | Content |
|---|---|---|---|
| A | angle A | S | tension S |
| B | angle B | T | tension T |
| C | sin(A+B) | W | weight |

***Exercise***

Calculate the tension assuming weight=40kg, angle A=30˚ 15' 20", and angle B=27˚ 45' 40". Enter the angles with sexagesimal numbers.

Set up condition: decimal point digit number in TAB 3 Mode, decimal point in Fix Mode, and angle unit in Deg Mode.

[2nd F] [SET UP] [C] [2] [D] [3] [B] [1] [CL]

| Step | Key Operation | Display |
|---|---|---|
| **1** Specify the programme mode. Select the title TENSION. | [PRGM] [A] | TENSION<br>Input ANGLE<br>A=? |
| **2** Enter the values of angles A and B. | [3] [0] [•] [1] [5] [2] [0] [ENTER]<br>[2] [7] [•] [4] [5] [4] [0] [ENTER] | Input ANGLE<br>A=<br>30.1520<br>B=<br>27.4540<br>Input WEIGHT<br>W=? |
| **3** Enter the value of weight. | [4] [0] [ENTER] | Input WEIGHT<br>W=<br>40<br>TENSION<br>T=<br>21.840<br>S=<br>23.795 |
| **4** Tension T is 21.840kg and S is 23.795kg. | | |

# Involute (Inverse Involute)

Use the involute function for calculating gears etc. to find the angle of obliquity from the initial value and involute value.
Conversely, calculate the involute value from the angle of obliquity.

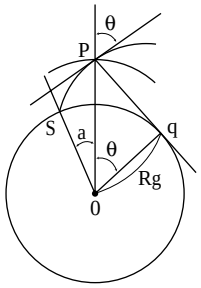
## *Calculation*

Involute function : inv θ = tan θ - θ[rad]
Use Newton's method to find the inverse involute:

$$\theta_{i+1} = \theta_i - \frac{f'(\theta)}{f(\theta_i)} = \theta_i - \frac{\tan\theta_i - \theta_i - a}{\tan^2\theta_i}$$

$f(\theta) = a - \text{inv}\theta$

SP : involute curve
S : involute starting point
θ : angle of obliquity of point P

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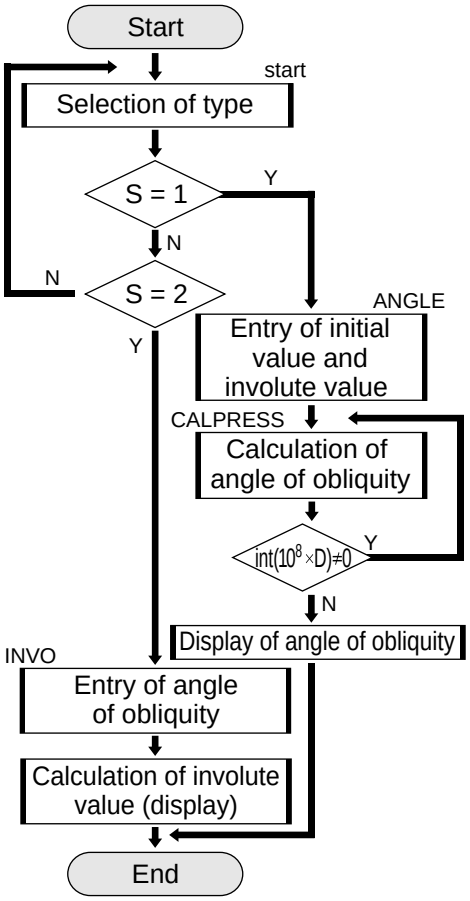



Enter 1 or 2.

To calculation of involute.

To inverse involute calculation
Returns to START if entry neither 1 nor 2.

Calculation of involute.
Enter initial value and involute value.

Angle of obliquity calculated.

Judgment on repetition of calculation of angle of obliquity.

Calculation of inverse involute. Enter angle of obliquity.

Involute value calculated.
Involute value displayed.

## PROGRAMME LIST (REAL MODE)

Title : INVOLUTE

```
Label START
ClrT
Print "SELECT 1 or 2
Input S
If S=1 Goto ANGLE
If S=2 Goto INVO
Goto START
Label ANGLE
Print "Input BEGIN
Input B
B ⇒ Z
Print "Input INVO
Input I
I ⇒ J
Label CALPRESS
tan Z ⇒ T
π*Z/180.0 ⇒ R
(T-R-J)/T^2 ⇒ D
180.0*(R-D)/π ⇒ Z
If int (10^8*D)≠0 Goto CALPRESS
Z ⇒ A
Print "ANGLE
Print A
End
Label INVO
Print "Input ANGLE
Input A
A ⇒ θ
tanθ -π*θ/180 ⇒ I
Print "INVOLUTE
Print I
End
```

## PARAMETERS

| Name of parameter | Content | Name of parameter | Content |
|---|---|---|---|
| D, R, T, J | working variable for calculating | θ | angle of obliquity |
| S | selecting calculation type | I | involute value |
| | (S=1: involute calculation) | A | input and output of angle |
| | (S=2: inverse involute calculation) | B | input of initial value |
| Z | initial value, angle of obliquity | | |

***Exercise***

(1) Find the angle of obliquity when the involute value is 0.0050912 and the initial value is 10.

(2) Find the involute value when the angle of obliquity is 14.1.

Set up condition: angle unit in Deg Mode and decimal point in Float Pt Mode.

[2nd F] [SET UP] [B] [1] [C] [1] [CL]

| Step | Key Operation | Display |
|---|---|---|
| **1** Specify the programme mode. Select the title INVOLUTE. | [PRGM] [A] | SELECT 1 or 2<br>S=? |
| **2** Select involute calculation. | [1] [ENTER] | SELECT 1 or 2<br>S=<br>1<br>Input BEGIN<br>B=? |
| **3** Enter the initial value and the involute value. | [1] [0] [ENTER]<br>[0] [•] [0] [0] [5] [0] [9] [1] [2]<br>[ENTER] | Input BEGIN<br>B=<br>10<br>Input INVO<br>I=<br>0.0050912<br>ANGLE<br>14.09998733 |
| (Display of angle of obliquity) | | |
| **4** Select inverse involute calculation. | [ENTER]<br>[2] [ENTER] | SELECT 1 or 2<br>S=<br>2<br>Input ANGLE<br>A=? |
| **5** Enter the value of the angle of obliquity. | [1] [4] [•] [1]<br>[ENTER] | SELECT 1 or 2<br>S=<br>2<br>Input ANGLE<br>A=<br>14.1<br>INVOLUTE<br>0.005091213 |
| (Display of involute value) | | |

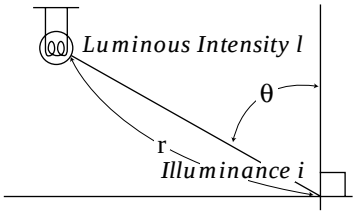
# Calculating Illuminance and Luminous Intensity

Enter the luminous intensity of the luminous source, the distance, and the angle between the perpendicular line and light ray, to find the illuminance of the illuminated side. Conversely, find the luminous intensity of the source from the illuminance of the illuminated side.

## Calculation

$$i = \frac{l \cdot \cos\theta}{r^2} \qquad l = \frac{r^2 \cdot i}{\cos\theta}$$

l : luminous intensity [candela]  i : illuminance [lux]
r : distance [m]  θ : angle [°]

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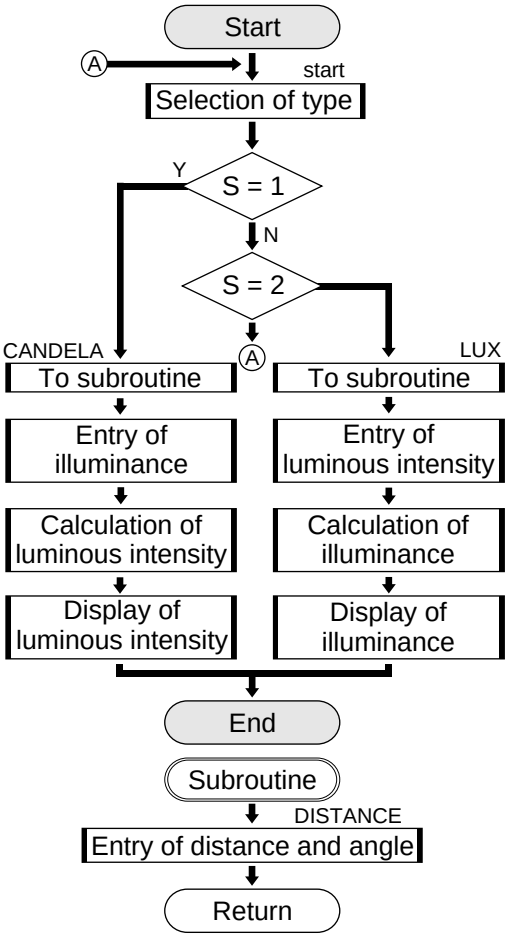



Enter 1 or 2.

To calculation of luminous intensity.

To calculation of illuminance.

Jumps to subroutine DISTANCE.

Enter illuminance or luminous intensity.

Illuminance or luminous intensity calculated.

Illuminance or luminous intensity displayed.

Subroutine for entry of distance and angle.

Entry.

Returns to calling program.

## PROGRAMME LIST (REAL MODE)

```
Title : CAND LUX
Deg
Label START
ClrT
Print "CANDELA=1 LUX=2
Print "SELECT 1 or 2
Input S
If S=1 Goto CANDELA
If S=2 Goto LUX
Goto START
Label CANDELA
Gosub DISTANCE
Print "Input LUX
Input L
L ⇒I
R²*I/cos θ⇒C
Print "CANDELA
Print C
End
Label LUX
Gosub DISTANCE
Print "Input CANDELA
Input C
C⇒K
K*cos θ /R² ⇒L
Print "LUX
Print L
End
Label DISTANCE
Print "Input DISTANCE
Input D
D⇒R
Print "Input ANGLE
Input A
A⇒θ
Return
```

## PARAMETERS

| Name of parameter | Content | Name of parameter | Content |
|---|---|---|---|
| I | illuminance of illuminated side | θ | angle |
| K | luminous intensity of luminous source | A | input of angle |
| R | distance | L | input and calculating luminous intensity |
| S | selecting calculation type (S=1: calculation of luminous intensity) (S=2: calculation of illuminance) | D | input of distance |
| | | C | input and calculating illuminance |

***Exercise***

(1) Find the luminous intensity of the luminous source of distance 10m, angle 60˚ and illuminance 20 lux.
(2) Find the illuminance of the illuminated side of distance 10m, angle 60˚ and luminous intensity 4000 candela.

Set up condition: decimal point in Float Pt Mode.

[2nd F] [SET UP] [C] [1] [CL]

| Step | Key Operation | Display |
|---|---|---|
| **1** Specify the programme mode. Select the title CAND LUX. | [PRGM] [A] | CANDELA=1 LUX=2<br>SELECT 1 or 2<br>S=? |
| **2** Select calculation of luminous intensity. | [1] [ENTER] | CANDELA=1 LUX=2<br>SELECT 1 or 2<br>S=<br>1<br>Input DISTANCE<br>D=? |
| **3** Enter the values of distance, angle, and illuminance. | [1] [0] [ENTER] [6] [0] [ENTER]<br>[2] [0] [ENTER] | CANDELA=1 LUX=2<br>SELECT 1 or 2<br>S=<br>1<br>Input DISTANCE<br>D=<br>10<br>Input ANGLE<br>A=<br>60<br>Input LUX<br>L=<br>20<br>CANDELA<br>4000 |
| **4** Select calculation of illuminance. Enter the values of distance, angle, and luminous intensity. | [ENTER] [2] [ENTER]<br>[1] [0] [ENTER]<br>[6] [0] [ENTER]<br>[4] [0] [0] [0] [ENTER] | Input ANGLE<br>A=<br>60<br>Input CANDELA<br>C=<br>4000<br>LUX<br>20 |

(Display of luminous intensity)

(Display of illuminance)

# Calculating Simple Harmonic Oscillation

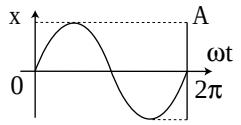
Enter period, amplitude and time to calculate displacement at specified time, acceleration, angular velocity, and velocity. Also, display the changes during the entered time period on a graph.

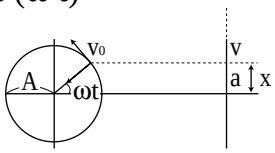
## *Calculation*

angular velocity : $\omega = \frac{2\pi}{T}$ displacement : $x = A \times \sin(\omega t)$

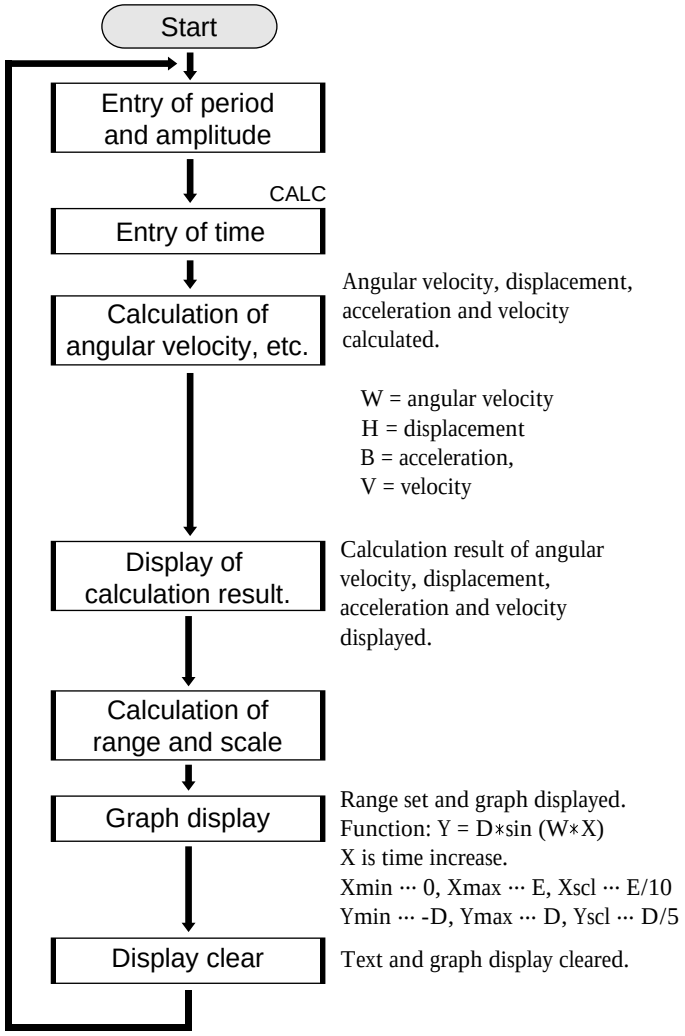
acceleration : $a = -\omega^2 \times x$ velocity : $v = A \times \omega \times \cos(\omega t)$

A : amplitude
t : time [sec]
T : period [sec]
ω : angular velocity [rad/sec]




## FLOWCHART




## PROGRAMME LIST(REAL MODE)

Title : OSCILLAT

```
Rad
Print "Input PERIOD
Input P
P⇒F
Print "Input AMPLITUDE
Input A
A⇒D
Label CALC
Print "Input TIME
Input T
T⇒E
2∗π/F⇒W
D∗sin (W∗E)⇒H
-(W²)∗H⇒B
D∗W∗cos (W∗E)⇒V
Print "ANGULAR VELOCITY
Print W
Print "MAGNITUDE
Print H
Print "ACCELERATION
Print B
Print "VELOCITY
Print V
Wait
E/10⇒X scl
D/5 ⇒Y scl
0⇒Xmin:E⇒Xmax
-D⇒Ymin:D⇒Ymax
Draw D∗sin (W∗X)
Wait
ClrT
ClrG
Goto CALC
```

## PARAMETERS

| Name of parameter | Content | Name of parameter | Content |
|---|---|---|---|
| B | acceleration | A | input of amplitude |
| E | time | P | input of period |
| V | velocity | T | input of time |
| W | angle of velocity (ω) | D | amplitude |
| H | displacement | F | period |
| Xscl | x-axis scale | X | time increase |
| Yscl | y-axis scale | | |

***Exercise***

Calculate angular velocity, etc., using period π, amplitude 1 and time 3 seconds and display the changes on a graph.

Set up condition: decimal point in Float Pt Mode.

2nd F SET UP C 1 E 1 CL

| Step | Key Operation | Display |
|---|---|---|
| **1** Specify the programme mode. Select the title OSCILLAT. | PRGM A | OSCILLAT<br>Input PERIOD<br>P=? |
| **2** Enter the values of period, amplitude, and time. | 2nd F π ENTER 1 ENTER 3 | OSCILLAT<br>Input PERIOD<br>P=<br>π<br>Input AMPLITUDE<br>A=<br>1<br>Input TIME<br>T=<br>3 |
| **3** (Display of angular velocity)<br>(Display of displacement)<br>(Display of acceleration)<br>(Display of velocity) | ENTER | ANGULAR VELOCITY<br>2<br>MAGNITUDE<br>-0.279415498<br>ACCELERATION<br>1.117661993<br>VEROCITY<br>1.920340573 |
| **4** (Display of graph of simple harmonic oscillation) | ENTER | |
| **5** | ENTER | Input TIME<br>T=? |

# Electric Power Consumed on an AC Circuit

Enter the voltage effective value, frequency and resistance value to find the power value of the circuit with resistance R. Draw a graph of the changes in power over a period of time.

## *Calculation*

P : power consumption  I : effective value of current

V : effective value of voltage

$I_0 = N \cdot \sin \omega \cdot t$  $V_0 = M \cdot \sin \omega \cdot t$  $P_0 = I_0 \cdot V_0$

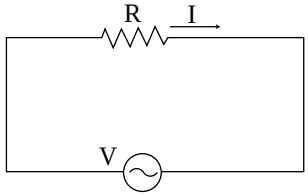
$P_0$ : change in amount of power with time

$I_0$ : change in amount of current with time

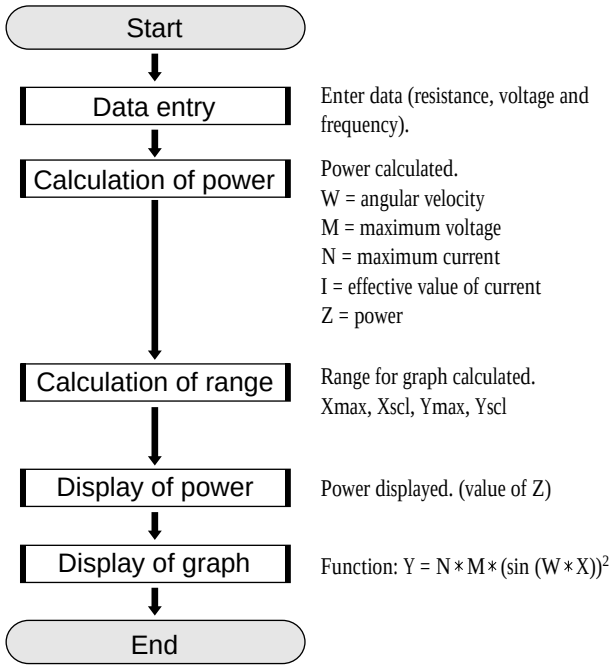
$V_0$: change in amount of voltage with time

N: maximum value of current  M: maximum value of voltage

$\omega$: angular velocity ($2 \pi S$)  t : time  S : frequency




## FLOWCHART




Enter data (resistance, voltage and frequency).

Power calculated.
W = angular velocity
M = maximum voltage
N = maximum current
I = effective value of current
Z = power

Range for graph calculated.
Xmax, Xscl, Ymax, Yscl

Power displayed. (value of Z)

Function: $Y = N * M * (\sin (W * X))^2$

## PROGRAMME LIST(REAL MODE)

Title : AC POWER

```
Rad
Print "Input RESISTANCE
Input R
Print "Input VOLTAGE
Input V
Print "Input FREQUENCY
Input F
R⇒T
V⇒D
F⇒ S
2∗π∗S ⇒W
D∗√2⇒ M
M/T⇒N
N/√2⇒I
D∗I⇒ Z
1/S ⇒ Xmax
Xmax/10⇒Xscl
N∗M⇒ Ymax
Ymax/10⇒Yscl
Print "WATT=
Print Z
Wait
0⇒Xmin
0⇒Ymin
Draw N∗M∗(sin (W∗X))^2
End
```

## PARAMETERS

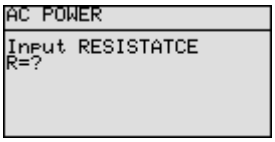
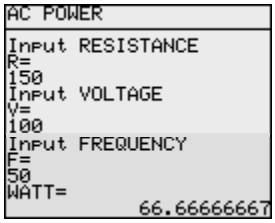
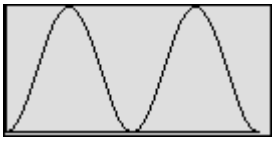
| Name of parameter | Content | Name of parameter | Content |
|---|---|---|---|
| S | frequency | Xscl | scale of x-axis |
| I | effective value of current | Ymax | maximum value of y-axis |
| T | resistance value | Yscl | scale of y-axis |
| D | effective value of voltage | V | input of voltage |
| W | angular velocity | R | input of resistance value |
| N | maximum value of current | F | input of frequency |
| M | maximum value of voltage | Z | value of power |
| Xmax | maximum value of x-axis | | |

***Exercise***

Find the power value of an AC circuit with resistance value 150Ω, voltage effective value 100V and frequency 50Hz and display on a graph the changes in power over a period of time.

Set up condition: decimal point in Float Pt Mode.

[2nd F] [SET UP] [C] [1] [E] [1] [CL]

| Step | Key Operation | Display |
|---|---|---|
| **1** Specify the programme mode. Select the title AC POWER. | [PRGM] [A] |  |
| **2** Enter the resistance value, voltage effective value, and frequency. | [1] [5] [0] [ENTER]<br>[1] [0] [0] [ENTER]<br>[5] [0] [ENTER] |  |
| (Display of value power) | | |
| **3** | [ENTER] |  |
| (Display of graph) | | |

# Angle of Vector

Use the matrix operation feature to find the angle θ which forms the standard vector and vector. The angle can be calculated at one time against the multiple vectors.

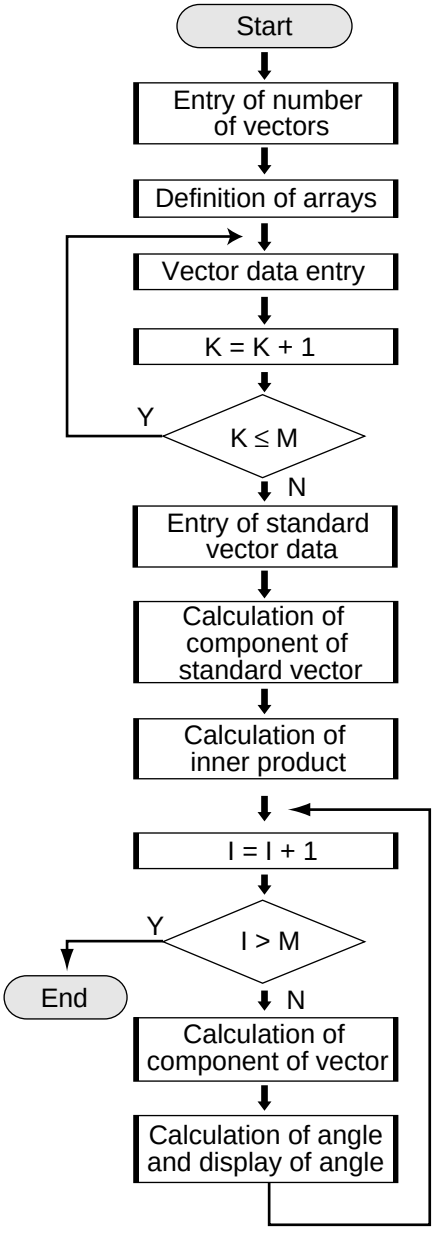
## *Calculation*

Calculating vector inner product $\vec{a}\cdot\vec{b} = |\vec{a}||\vec{b}|\cos\theta$

Use the above expression to derive the following expression

$$\theta = \cos^{-1}\frac{\vec{a}\cdot\vec{b}}{|\vec{a}||\vec{b}|}$$

## FLOWCHART




## PROGRAMME LIST (MATRIX MODE)

Title : VECTOR

```
Print " Input NUMBER
Input N
N⇒M
{M,2}⇒dim  (mat A)
{2,1} ⇒dim  (mat B)
{M,1}⇒dim  (mat C)
For K, 1, M, 1
Print " Input VECTOR
Print K
Input X
X⇒mat  A(K,1)
Input Y
Y⇒mat  A(K,2)
NEXT
Print "Input FUNDAMENTAL VECTOR
Input  X
X⇒mat   B(1,1)
Input  Y
Y⇒mat  B(2,1)
√ (mat  B(1,1)²+mat  B(2,1)²)⇒B
mat  A∗mat  B⇒mat  C
For I, 1, M, 1
√ (mat  A(I,1)²+mat  A(I,2)²)⇒A
cos⁻¹  (mat  C(I,1) / (A∗B))⇒θ
Print "ANGLE OF VECTOR
Print I
Print "θ=
Print θ
Wait
NEXT
End
```

## PARAMETERS

| Name of parameter | Content | Name of parameter | Content |
|---|---|---|---|
| A | vector scalar quantity | θ | vector angle |
| B | standard vector scalar quantity | K | display |
| I | calculating counter | N | input of number of vectors |
| K | input counter | mat A | vector components |
| M | number of vectors | mat B | standard vector components |
| X | input of x component | mat C | vector inner product |
| Y | input of y component | | |

***Exercise***

Calculate the angle formed by the following 3 vectors and standard vector (2,3).
vector 1 (5, 8)
vector 2 (7, 4)
vector 3 (9, 2)

Set up condition: angle unit in Deg mode, and decimal point in Float Pt mode.

[2nd F] [SET UP] [B] [1] [C] [1] [CL]

| Step | Key Operation | Display |
|---|---|---|
| **1** Specify the programme mode. Select the title VECTOR. | [PRGM] [A] | VECTOR<br>Input NUMBER<br>N=? |
| **2** Enter the number of vectors. | [3] [ENTER] | VECTOR<br>Input NUMBER<br>N=<br>3<br>Input VECTOR 1<br>X=? |
| **3** Enter the values of vector 1. | [5] [ENTER] [8] [ENTER] | 1<br>X=<br>5<br>Y=<br>8<br>Input VECTOR 2<br>X=? |
| **4** Enter the values of vectors 2 and 3. | [7] [ENTER] [4] [ENTER]<br>[9] [ENTER] [2] [ENTER] | 3<br>X=<br>9<br>Y=<br>2<br>Input FUNDAMENTAL VECTOR<br>X=? |
| **5** Enter the value of standard vector.<br>(Display of angle of vector 1) | [2] [ENTER] [3] [ENTER] | X=<br>2<br>Y=<br>3<br>ANGLE OF VECTOR 1<br>θ=<br>1.684684318 |
| **6** (Display of angle of vector 2) | [ENTER] | ANGLE OF VECTOR 2<br>θ=<br>26.56505118 |
| (Display of angle of vector 3) | [ENTER] | ANGLE OF VECTOR 3<br>θ=<br>43.78112476 |

# Linear Transformation

Use the matrix to find four types of the linear transformation of x-axis symmetric transformation, y-axis symmetric transformation, similar transformation and revolution around the origin.

## *Calculation*

1. Symmetric transformation to x-axis (Case 1)

$$\begin{pmatrix} X' \\ Y' \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix}$$

2. Symmetric transformation to y-axis (Case 2)

$$\begin{pmatrix} X' \\ Y' \end{pmatrix} = \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix}$$

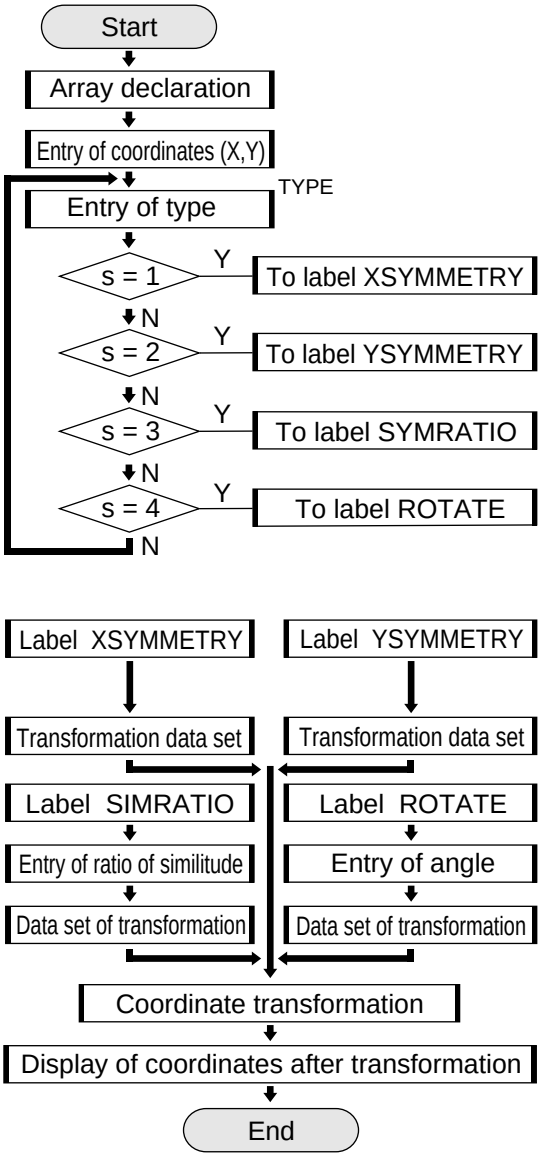
3. Similar transformation with ratio of similitude K around origin (Case 3)

$$\begin{pmatrix} X' \\ Y' \end{pmatrix} = \begin{pmatrix} K & 0 \\ 0 & K \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix}$$

4. Transformation revolving around only angle B at the origin (Case 4)

$$\begin{pmatrix} X' \\ Y' \end{pmatrix} = \begin{pmatrix} \cos B & -\sin B \\ \sin B & \cos B \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix}$$

## FLOWCHART




Declare array size, etc.
matH(2,2), matD(2,1), matA(2,1)

Enter coordinates before transformation.

Type of transformation specified with no from 1 to 4.

Jumps to destination corresponding to entered number.

XSYMMETRY
Data set of x-axis symmetric transformation
matH(1,1) = 1, matH(1,2) = 0,
matH(2,1) = 0, matH(2,2) = -1

YSYMMETRY
Data set of y-axis symmetric transformation
matH(1,1) = -1, matH(1,2) = 0,
matH(2,1) = 0, matH(2,2) = 1

SIMRATIO
Data set of similar transformation
Entry of ratio of similitude (R)
matH(1,1) = K, matH(1,2) = 0,
matH(2,1) = 0, matH(2,2) = θ

Data set of transformation by revolving
Entry of angle (A)
matH(1,1) = cos B, matH(2,1) = sin B,
matH(1,2) = -sin B, matH(2,2) = cos B,

Matrix H multiplied by matrix D.

Coordinates displayed.

## PROGRAMME LIST

Title : LINE TRN

```
{2, 2}⇒dim(mat H)
{2, 1}⇒dim(mat D)
{2, 1}⇒dim(mat A)
Print "Input POINT
Input X
Input Y
X ⇒mat D(1, 1)
Y ⇒mat D(2, 1)
Label TYPE
Print "SELECT 1, 2, 3, 4
Input S
ClrT
If S=1 Goto XSYMMETRY
If S=2 Goto YSYMMETRY
If S=3 Goto SIMRATIO
If S=4 Goto ROTATE
GotoTYPE
Label XSYMMETRY
1 ⇒mat H(1, 1)
0 ⇒mat H(2, 1)
0 ⇒mat H(1, 2)
-1⇒ mat H(2, 2)
Goto TRANS
Label YSYMMETRY
-1 ⇒mat H(1, 1)
0 ⇒mat H(2, 1)
0 ⇒mat H(1, 2)
1 ⇒mat H(2, 2)
Goto TRANS
Label SIMRATIO
Print "Input SIMILITUDE RATIO
Input R
R ⇒K
K ⇒mat H(1, 1)
0 ⇒mat H(2, 1)
0 ⇒mat H(1, 2)
θ ⇒mat H(2, 2)
Goto TRANS
Label ROTATE
Print "Input ANGLE
Input A
A ⇒B
cos B⇒ mat H(1, 1)
sin B ⇒mat H(2, 1)
-sin B⇒ mat H(1, 2)
cos B⇒ mat H(2, 2)
Label TRANS
mat H∗mat D⇒ mat A
Print "mat A(1, 1)
Print mat A(1, 1)
Print "mat A(2, 1)
Print mat A(2, 1)
End
```



SHARP

## PARAMETERS

| Name of parameter | Content | Name of parameter | Content |
|---|---|---|---|
| B | angle | Y | y-coordinate |
| K | ratio of similitude | A | input of angle |
| S | selecting type | R | input of ratio of similitude |
| | (S=1: case 1, S=2: case 2, | mat A | coordinate after transformation |
| | S=3: case 3, S=4: case 4) | mat H | transformation data |
| X | x-coordinate | mat D | x,y-coordinate |

***Exercise***

1. Transform symmetrically the point (3, 5) to the x-axis.
2. Rotate the point (2, 6) at 45˚ around the origin.

Set up condition: angle unit in Deg Mode and decimal point in Float Pt Mode.

[2nd F] [SET UP] [B] [1] [C] [1] [CL]

| Step | Key Operation | Display |
|---|---|---|
| **1** Specify the programme mode. Select the title LINE TRN. | [PRGM] [A] | LINE TRN<br>Input POINT<br>X=? |
| **2** Enter the values of the point. | [3] [ENTER] [5] [ENTER] | Input POINT<br>X=<br>3<br>Y=<br>5<br>SELECT 1,2,3,4<br>S=? |
| **3** Select symmetric transformation to x-axis (case 1). | [1] [ENTER] | mat A(1,1) 3<br>mat A(2,1) -5 |
| **4** Select transformation revolving around only angle B at the origin (case 4). | [ENTER] [2] [ENTER] [6] [ENTER] [4] | Input POINT<br>X=<br>2<br>Y=<br>6<br>SELECT 1,2,3,4<br>S=<br>4 |
| **5** Enter the angle value. | [ENTER] [4] [5] [ENTER] | Input ANGLE<br>A=<br>45<br>mat A(1,1) -2.828427125<br>mat A(2,1) 5.656854249 |

# Moving Average

Plot a moving average graph which helps to understand how the results change over a specified period. The progress of sales and amounts of consumption and production can also be seen.

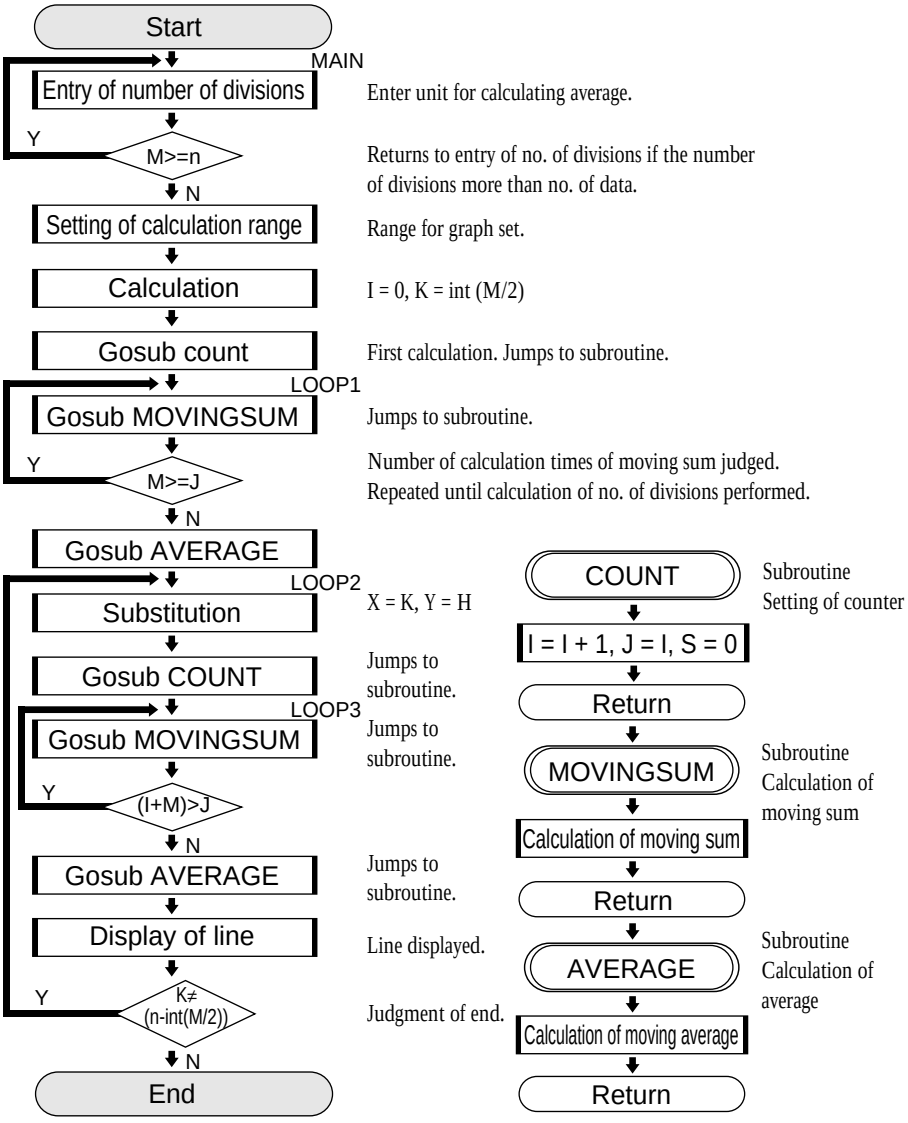
## Calculation

$$H_i = \frac{X_{i-(M-1)/2} + \ldots + X_i + \ldots X_{i+(M-1)/2}}{M}$$

$$\left( I = 1 + \frac{M-1}{2}, 2 + \frac{M-1}{2}, \ldots, n + \frac{M-1}{2} \right)$$

$H_i$ : moving average
M : number of divisions
$X_i$ : data
n : number of data

## FLOWCHART




## PROGRAMME LIST

Title : MVIN AVG

```
Label MAIN
Print "Input DIVISION
Input D
D⇒M
1_Stats L1
If M≥n Goto MAIN
Rem RANGE
(xmax-xmin)/10⇒Yscl
0⇒Xmin
n⇒Xmax
1⇒Xscl
xmin⇒Ymin
xmax⇒Ymax
0⇒I
int (M/2)⇒K
Gosub COUNT
Label LOOP1
Gosub MOVINGSUM
If M≥J Goto LOOP1
Gosub AVERAGE
Label LOOP2
K⇒X
H⇒Y
Gosub COUNT
Label LOOP3
Gosub MOVINGSUM
If (I+M)>J Goto LOOP3
Gosub AVERAGE
Line (X, Y, K, H)
If K≠(n-int (M/2))Goto LOOP2
Wait
End
Label COUNT
I+1⇒I
I⇒J
0⇒S
Return
Label MOVINGSUM
S+L1(J)⇒S
J+1⇒J
Return
Label AVERAGE
S/M⇒H
K+1⇒K
Return
```

## Parameters

| name of parameter | content | name of parameter | content |
|---|---|---|---|
| H | moving average | S | moving sum |
| I | counter | X | starting point (x) |
| J | counter | Y | starting point (y) |
| K | counter | Yscl | scale of y-axis |
| M | number of divisions | B | input of number of divisions |

### *Exercise*

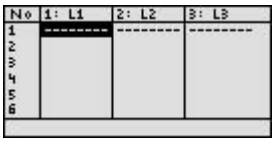
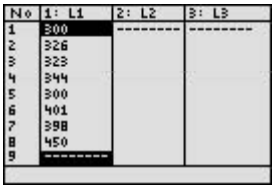
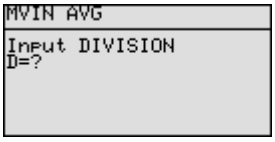
Find the moving average every three months (number of divisions: 3) from the following table of monthly sales.

| Month | Jan. | Feb. | Mar. | Apr. | May. | Jun. | Jul. | Aug. |
|---|---|---|---|---|---|---|---|---|
| Sales[$] | 300 | 326 | 323 | 344 | 300 | 401 | 398 | 450 |

On the graph, Xmax = 8, Ymin = 300, and Ymax = 450.

Set up condition: decimal point in Float Pt Mode.

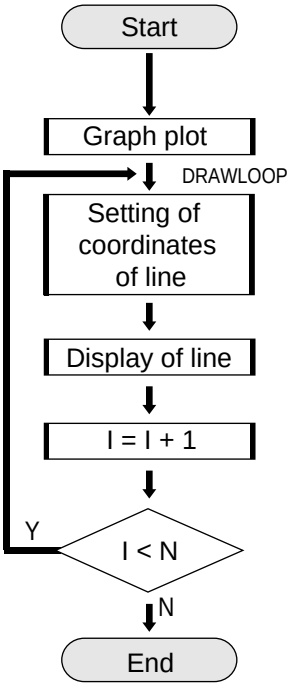
[2nd F] [SET UP] [C] [1] [CL]

| *Step* | *Key Operation* | *Display* |
|---|---|---|
| **1** Enter statistical data into L1. | [STAT] [A] [ENTER] |  |
| | [3] [0] [0] [ENTER] [3] [2] [6] [ENTER] [3] [2] [3] [ENTER] [3] [4] [4] [ENTER] [3] [0] [0] [ENTER] [4] [0] [1] [ENTER] [3] [9] [8] [ENTER] [4] [5] [0] [ENTER] |  |
| **2** Specify the programme mode. Select the title MVIN AVG. | [PRGM] [A] | |
| **3** Enter the number of divisions(3). | [3] [ENTER] |  |

# Creating a Graph of Experimental Data

Graph the results of an experiment and examine the trends.
(Example: examined data relating to water vapour pressure and temperature.)

## FLOWCHART




Enter statistical data using statistics feature before executing program.

Graph plotted using automatic scaling.

Counter

Data as coordinates (starting point and finishing point).

Line drawn between set coordinates.

Whether or not lines of no. of data drawn judged. Repeated until lines drawn by the no. of data.

## PROGRAMME LIST

Title : XY GRAPH

```
ClrG
Rem DRAWING SD
2 -Stats L1,L2
Rem RANGE
xmin⇒Xmin
xmax ⇒ Xmax
ymin ⇒ Ymin
ymax⇒Ymax
(Xmax-Xmin) / 10⇒Xscl
(Ymax-Ymin) / 10⇒Yscl
Rem BROKEN LINE
For I, 1, n-1, 1
L1(I)⇒X
L2(I)⇒Y
L1(I+1)⇒Z
L2(I+1)⇒W
Line(X,Y,Z,W)
NEXT
Wait
End
```

## PARAMETERS

| Name of parameter | Content | Name of parameter | Content |
|---|---|---|---|
| I | counter | Y | y of line starting point |
| X | x of line starting point | W | y of line finishing point |
| Z | x of line finishing point | | |

*n = number of statistical data

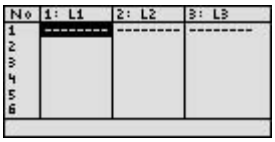
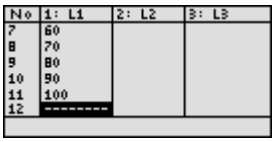
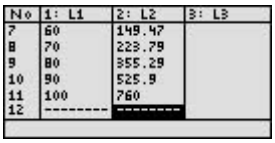
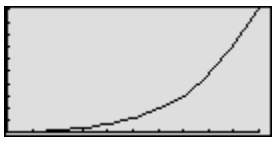
***Exercise***

The following table shows examined water vapour pressure. Draw a graph of this data.

| Temperature [˚C] | 0 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 |
|---|---|---|---|---|---|---|---|---|---|---|---|
| Pressure [mmHg] | 4.581 | 9.205 | 17.532 | 31.826 | 55.339 | 92.558 | 149.47 | 223.79 | 355.29 | 525.90 | 760.00 |

Set up condition: decimal point in Float Pt Mode.

2nd F SET UP C 1 CL

| Step | Key Operation | Display |
|---|---|---|
| **1** Enter statistical data into L1 and L2. | STAT A ENTER |  |
| **2** Enter the value for temperature. | 0 ENTER 1 0 …<br>1 0 0 ENTER<br>(Other numbers not shown) |  |
| **3** Enter the value for pressure. | ▶ 4 • 5 8 1 ENTER<br>… 7 6 0 ENTER |  |
| **4** Specify the programme mode. Select the title XY GRAPH.<br>(Drawing of graph) | PRGM A |  |

# Ordinary Differential Equations

Enter the initial conditions (X, Y) with the step H and interval T. Use Runge Kutta Gill method to solve the ordinary differential equation of first order.

## *Calculation*

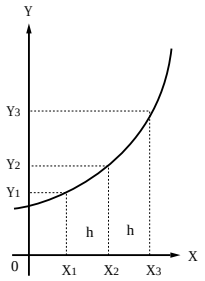
Use the following four steps of Runge Kutta Gill method to find the equation $X_{n+1}$ and $Y_{n-1}$ from $X_n$ and $Y_n$. Input $Q_0 = 0$ at the starting point $X_0$.

1. $K_0 = Hf(X_n, Y_n)$, $R1 = (1/2)(K_0 - 2Q_0)$, $Y^{(1)} = Y_n + R_1$

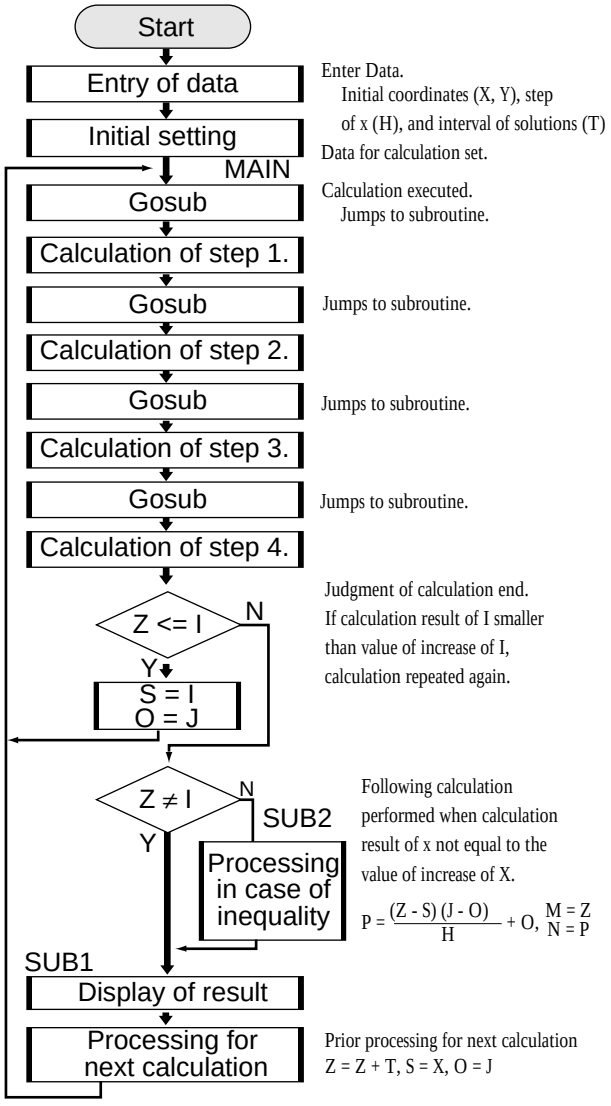
2. $Q_1 = Q_0 + 3R_1 - (1/2)K_0$
   $K_1 = Hf(X_n + H/2, Y^{(1)})$, $R_2 = (1 - \sqrt{1/2})(K_1 - Q_1)$, $Y^{(2)} = Y^{(1)} + R_2$

3. $Q_2 = Q_1 + 3R_2 - (1 - \sqrt{1/2})K_1$
   $K_2 = Hf(Xn + H/2, Y^{(2)})$, $R_3 = (1 + \sqrt{1/2})(K_2 - Q_2)$, $Y^{(3)} = Y^{(2)} + R_3$

4. $Q_3 = Q_2 + 3R_3 - (1 + \sqrt{1/2})K_2$
   $K_3 = Hf(X_{n+1}, Y^{(3)})$, $R_4 = (1/6)(K_3 - 2Q_3)$, $Y_{n+1} = Y^{(3)} + R_4$
   $Q_4 = Q_3 + 3R_4 - (1/2)K_3$




## FLOWCHART




Enter Data.
Initial coordinates (X, Y), step of x (H), and interval of solutions (T)
Data for calculation set.

Calculation executed.
Jumps to subroutine.

Jumps to subroutine.

Jumps to subroutine.

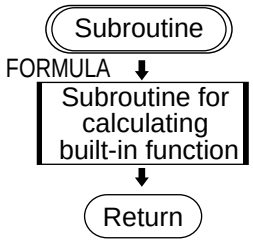
Jumps to subroutine.

Judgment of calculation end.
If calculation result of I smaller than value of increase of I, calculation repeated again.

Following calculation performed when calculation result of x not equal to the value of increase of X.

$$P = \frac{(Z - S)(J - O)}{H} + O, \quad \begin{matrix} M = Z \\ N = P \end{matrix}$$

Prior processing for next calculation
Z = Z + T, S = X, O = J




Subroutine for calculating built-in function

f = -I ∗J
(Another equation can be used.)

## PROGRAMME LIST(REAL MODE)

Title : RUNGE

```
Rem INITIAL
Print " Input X0
Input X
Print " Input Y0
Input Y
X⇒I
Y⇒J
Print " Input H
Input H
Print " Input T
Input T
1+√(2^-1)⇒A
1- √(2^-1)⇒B
I+T⇒Z
O⇒Q
I⇒S
Label MAIN
Rem 1
Gosub FORMULA
H∗F⇒K
(K-2∗Q) /2⇒R
J+R⇒J
Q+3∗R-K/2⇒Q
I+H/2⇒I
Rem 2
Gosub FORMULA
H∗F⇒K
B∗(K-Q)⇒ R
J+R⇒J
Q+3∗R-B∗K⇒Q
Rem 3
Gosub FORMULA
H∗F⇒K
A∗(K-Q)⇒ R
J+R⇒J
Q+3∗R - A∗K⇒Q
I+H/2⇒I
Rem 4
Gosub FORMULA
H∗F⇒K
(K - 2∗Q) /6⇒R
J+R⇒J
Q+3∗R - K/2⇒Q
If Z≤I Goto NEXT
I⇒S
J⇒O
Goto MAIN
Label NEXT
If Z≠I Goto SUB2
I⇒M
J⇒N
Label SUB1
ClrT
Print "XN=
Print M
Print "YN=
Print N
Wait
Z+T⇒Z
I⇒S
J⇒O
Goto MAIN
Label SUB2
(Z-S)∗(J-O) /H+O⇒P
Z⇒M
P⇒N
Goto SUB1
Label FORMULA
-I∗J⇒F
Return
```

## PARAMETERS

| Name of parameter | Content | Name of parameter | Content |
|---|---|---|---|
| A | value of $1+\sqrt{(1/2)}$ | S | value of Xn-1 |
| B | value of $1-\sqrt{(1/2)}$ | T | interval |
| F | f (I,J) | I | Xn |
| H | step | J | Yn |
| K | calculating working area | Z | value of increase of X |
| O | value of Yn-1 | X | input of $X_0$ |
| P | increase of J | Y | input of $Y_0$ |
| Q | value of Qn | M | indicates Xn |
| R | value of Rn | N | indicates Yn |

***Exercise***

Initial settings: Y = 10 when X = 0. Find J when H = 0.01, T = 0.03 and I = 0.03, 0.06···.
(The built-in differential equation is F = -I ∗ J.)

Set up condition: angle unit in Rad Mode and decimal point in Float Pt Mode.

[2nd F] [SET UP] [B] [2] [C] [1] [CL]

| ***Step*** | ***Key Operation*** | ***Display*** |
|---|---|---|
| **1** Specify the programme mode. Select the title RUNGE. | [PRGM] [A] | RUNGE<br>Input X0<br>X=? |
| **2** Enter the values of $X_0$, $Y_0$, H and T. | [0] [ENTER] [1] [0] [ENTER]<br>[0] [•] [0] [1] [ENTER]<br>[0] [•] [0] [3] | RUNGE<br>Input X0<br>X=<br>0<br>Input Y0<br>Y=<br>10<br>Input H<br>H=<br>0.01<br>Input T<br>T=<br>0.03 |
| **3** (Display of X1)<br>(Display of Y1) | [ENTER] | XN= 0.03<br>YN= 9.995501012 |
| **4** (Display of X2)<br>(Display of Y2) | [ENTER] | XN= 0.06<br>YN= 9.98201619 |
| **5** (Display of X3)<br>(Display of Y3) | [ENTER] | XN= 0.09<br>YN= 9.959581902 |

Similar operation is performed hereafter.

# Analysing with One-way Layout Method

Use the one-way layout method to verify whether there is a relation to the results achieved based on one condition. Analysis of variance is carried out with this method.

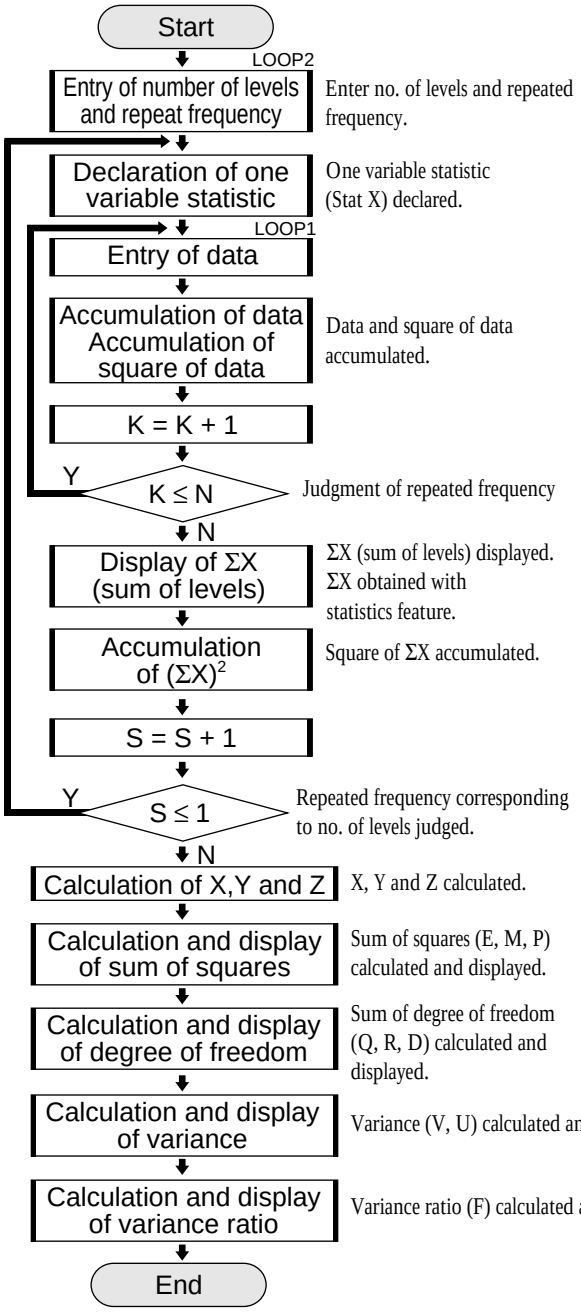
## *Calculation*

Analysis of variance chart of one-way layout method

| | Sum of squares (S) | Degree of freedom (θ) | Variance (V) | Variance ratio (F) |
|---|---|---|---|---|
| Factor | $S_A = [A] - [X]$ | $\theta_A = A - 1$ | $V_A = S_A \div \theta_A$ | $F_A = V_A \div V_E$ |
| Error | $S_E = [AS] - [A]$ | $\theta_E = A (N - 1)$ | $V_E = S_E \div \theta_E$ | |
| Total | $S_T = [AS] - [X]$ | $\theta_T = AN - 1$ | | |

$[X] = (\Sigma\ \Sigma\ Xij)^2 \div AN$
$[A] = \Sigma i\ (\Sigma j\ Xij)^2 \div N$
$[AS] = \Sigma i\ \Sigma j\ (Xij)^2$
A : number of levels
N : repeated frequency
X : number of data

## FLOWCHART




## PROGRAMME LIST(STAT MODE)

Title : VARIANCE

```
Rem INPUT
Print "Input LEVEL
Input L
L⇒A
Print "Input TIMES
Input T
T⇒N
0⇒W
0⇒B
0⇒C
For S, 1, A, 1
N⇒dim(L1)
For K, 1, N, 1
ClrT
S⇒L
K⇒T
Print "Input DATA
Print "LEVEL
Print L
Print "TIME
Print T
Input I
I⇒L1(K)
B+I⇒B
C+I²⇒C
NEXT
1_Stats L1
Σx⇒J
Print "Σx=
Print J
Wait
W+(Σx)²⇒W
NEXT
Rem CALCULATE
B²/A/N⇒X
W/N⇒Y
C⇒Z
Rem SUM OF SQUARES
Y-X⇒E
Z-Y⇒M
Z-X⇒P
Print "SUM OF SQUARES
Print E
Print "ERROR SUM OF SQUARES
Print M
Wait
Print "TOTAL SUM OF SQUARES
Print P
Wait
Rem DEGREES OF FREEDOM
A-1⇒Q
A*(N-1)⇒R
A*N-1⇒D
Print "DEGREES OF FREEDOM
Print Q
Print "DEGREES OF FREEDOM
Print R                    ↳ABOUT ERRORS
Wait
Print "SUM OF DEGREES OF FREEDOM
Print D
Wait
Rem VARIANCE
E/Q⇒V
M/R⇒U
Print "VARIANCE
Print V
Print "VARIANCE OF ERRORS
Print U
Wait
Rem VARIANCE RATIO
V/U⇒F
Print "VARIANCE RATIO
Print F
End
```



SHARP

## PARAMETERS

| Name of parameter | Content | Name of parameter | Content |
|---|---|---|---|
| A | number of levels | V | variance factor |
| I | input of data | U | variance error |
| K | loop 1 counter | Y | $\Sigma i\ (\Sigma\ jxij)^2 / n$ |
| J | indicating $\Sigma x$ | Q | degree of freedom factor |
| N | repeated frequency | R | degree of freedom error |
| S | loop 2 counter | D | degree of freedom total |
| X | $(\Sigma\Sigma\ xi)^2 / a / n$ | T | input and indicating frequency |
| Z | $\Sigma i\ \Sigma j\ (xij)^2$ | L | input and indicating number of levels |
| F | variance ratio factor | W | total sum of squares of each level |
| E | sum of squares factor | B | total sum (all data) |
| M | sum of squares error | C | total sum of squares (all data) |
| P | sum of squares total | | |

### *Exercise*

When a mouse is given a dosage of hormone, the relationship between dosage amount and increase of mouse weight is as shown in the following table. Find the analysis of variance. If the value of the variance ratio is larger than the value of the F- distribution table at the 5% level of significance, the relationship between the hormone amount and the increase of mouse weight is a causal relation.

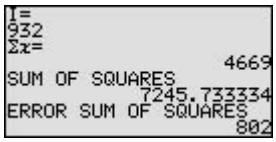
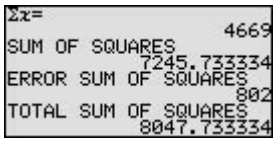
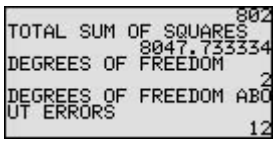
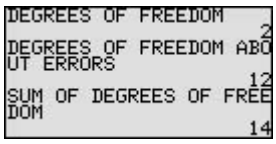
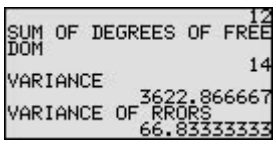
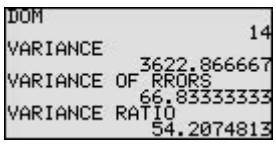
| | Increase mouse weight (grams/day) | | | | | |
|---|---|---|---|---|---|---|
| | | 10 | 20 | 30 | 40 | 50 |
| Hormone (grams/mouse) | 10 | 882 | 891 | 864 | 888 | 885 |
| | 20 | 923 | 915 | 923 | 912 | 930 |
| | 30 | 933 | 939 | 925 | 940 | 932 |

The number of levels (number of columns in the table) is A = 3
The repeated frequency (number of rows in the table ) is N = 5

Set up condition: decimal point in Float Pt Mode.

[2nd F] [SET UP] [C] [1] [CL]

| Step | Key Operation | Display |
|---|---|---|
| **1** Specify the programme mode. Select the title VARIANCE. | [PRGM] [A] | VARIANCE<br>Input LEVEL<br>L=? |
| **2** Enter the number of levels and the repeated frequency. | [3] [ENTER] [5] | VARIANCE<br>Input LEVEL<br>L=<br>3<br>Input TIMES<br>T=<br>5 |
| **3** | [ENTER] | Input DATA<br>LEVEL 1<br>TIME 1<br>I=? |

| Step | Key Operation | Display |
|---|---|---|
| **4** Enter the statistical data in level 1. | 8 8 2 ENTER 8 9 1 ENTER 8 6 4 ENTER 8 8 8 ENTER 8 8 5 ENTER | |
| (Display of total of hormone 10 g) | | |
| **5** Enter the statistical data in level 2. | ENTER 9 2 3 ENTER 9 1 5 ENTER 9 2 3 ENTER 9 1 2 ENTER 9 3 0 ENTER | |
| (Display of total of hormone 20 g) | | |
| **6** Enter the statistical data in level 3. | ENTER 9 3 3 ENTER 9 3 9 ENTER 9 2 5 ENTER 9 4 0 ENTER 9 3 2 ENTER | |
| (Display of total of hormone 30 g) | | |
| **7** | ENTER |  |
| (Display of sum of squares)<br>(Display of error sum of squares) | | |
| **8** | ENTER |  |
| (Display of sum of squares) | | |
| **9** | ENTER |  |
| (Display of degrees of freedom)<br>(Display of degrees of freedom about errors) | | |
| **10** | ENTER |  |
| (Display of sum of degrees of freedom) | | |
| **11** | ENTER |  |
| (Display of variance)<br>(Display of variance of errors) | | |
| **12** | ENTER |  |
| (Display of variance ratio) | | |

The F-distribution chart shows that the value of F of upper probability P = 5% is 3.89. Since f > 3.98 in this example, the relationship between the hormone amount and the increase of mouse weight is a causal relation with 5% level of significance.

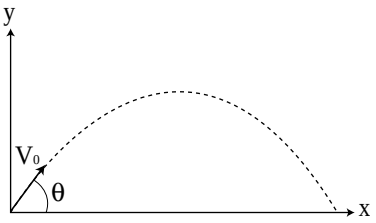
# Calculating Parabolic Motion

Display on a graph the altitude change and the horizontal distance over a period of time when an object is thrown at initial velocity $V_0$ and angle θ, and find the horizontal distance and altitude after t seconds. Specify the angle in Deg.

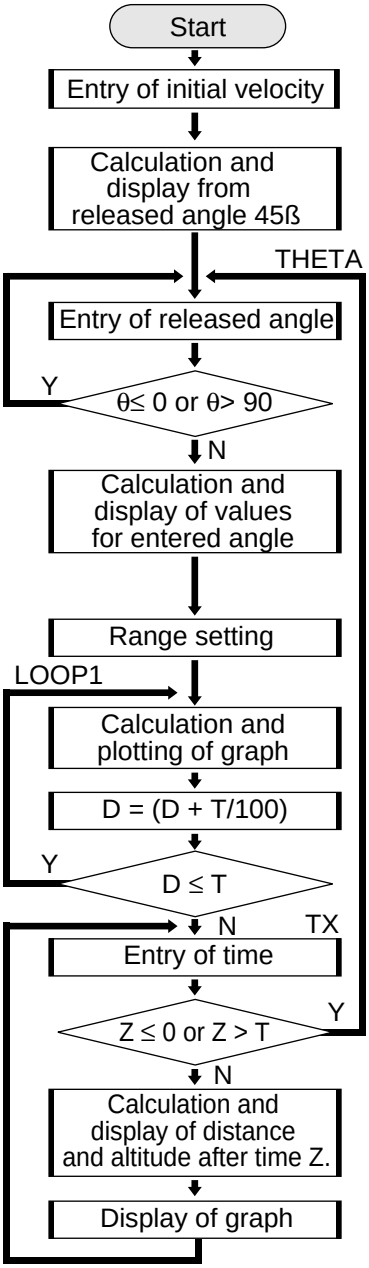
## *Calculation*

$X = V_0 \cdot \cos\theta \cdot T \qquad Y = V_0 \cdot \sin\theta \cdot T - \frac{1}{2} gT^2$

| | |
|---|---|
| Initial velocity | $V_0$ [m/s] |
| Angle | θ [˚ ] |
| Gravitational acceleration | g = 9.8 [m/s²] |
| Time | T [s] |




## FLOWCHART




Enter velocity when thrown.

Highest altitude, throwing distance (horizontal distance), and time (duration of flight) in case of released angle 45˚ calculated and displayed.

Angle for throwing entered.

Entered angle less than or equal to 0˚ or larger than 90˚?

Highest altitude, throwing distance (horizontal distance), and time (duration of flight) for entered angle calculated and displayed.

Range of graph set based on values for released angle 45˚.

Graph (parabola) calculated and plotted.

Elapsed time counted.

Calculation and plotting repeated until D (time elapsed) reaches T (duration of flight).

Entered time less than or equal to 0 or more than T?

Altitude and distance after entered time elapses from throwing calculated and displayed.

Returns to entry of time.

## PROGRAMME LIST(REAL MODE)

Title : PARABOLA

```
Deg
Print "V0 (M÷S),θ,T(S)
Print "Input V0
Input V
2∗V∗sin 45/9.8⇒A
V²/9.8⇒B
V²/19.6⇒C
Print "HMAX=
Print C
Print "LMAX=
Print B
Print "TMAX=
Print A
Wait
Label THETA
Input θ
If θ ≤ 0 Goto THETA
If θ > 90 Goto THETA
V²∗(sin θ)²/19.6⇒H
V²∗sin (2θ)/9.8⇒L
2∗V∗sin θ/9.8⇒T
Print "H=
Print H
Print "L=
Print L
Print "T=
Print T
Wait
C/10⇒Yscl
B/10⇒Xscl
0⇒Xmin
0⇒Ymin
B⇒Xmax
C⇒Ymax
For D, 0, T, T/100
V∗cos θ∗D⇒X
V∗sin θ∗D-(0.5∗9.8∗D²)⇒Y
Pnt0N(X,Y)
NEXT
Wait
Label TX
Print "Input TX
Input Z
If Z≤0 Goto THETA
If Z>T Goto THETA
V∗cos θ∗Z⇒X
V∗sin θ∗Z-(0.5∗9.8∗Z²)⇒Y
Print "X=
Print X
Print "Y=
Print Y
Wait
Line(0,Y,X,Y)
Line(X,0,X,Y)
Wait
Goto TX
```

## PARAMETERS

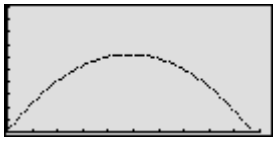
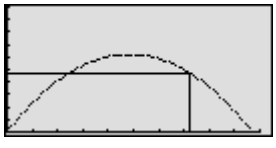
| Name of parameter | Content | Name of parameter | Content |
|---|---|---|---|
| H | highest altitude | Xscl | scale of x-coordinate |
| L | horizontal distance | Z | input of time period |
| T | time | V | initial velocity ($V_0$) |
| X | distance (after time Z) | θ | angle (released angle) |
| Y | altitude (after time Z) | C | highest altitude when released at 90° |
| D | time elapsed | B | horizontal distance when released at 45° |
| Yscl | scale of y-coordinate | A | time period when released at 45° |

### *Exercise*

Find the horizontal distance and altitude three seconds after an object is thrown, when the initial velocity is 25m/sec and the angle is 52°.

Set up condition: angle unit in Deg mode, and decimal point in Float Pt mode.

[2nd F] [SET UP] [B] [1] [C] [1] [E] [1] [CL]

| Step | Key Operation | Display |
|---|---|---|
| **1** Specify the programme mode. Select the title PARABOLA. | [PRGM] [A] | PARABOLA<br>V0(M/S),θ,T(S)<br>Input V0<br>V= |
| **2** Enter the value of the initial velocity.<br>(Highest altitude when released at 90°)<br>(Distance when released at 45°)<br>(Time when released at 45°) | [2] [5] [ENTER] | V=<br>25<br>HMAX= 31.8877551<br>LMAX= 63.7755102<br>TMAX= 3.607687659 |
| **3** | [ENTER] | 25<br>HMAX= 31.8877551<br>LMAX= 63.7755102<br>TMAX= 3.607687659<br>θ=? |
| **4** Enter the angle value.<br>(Display of highest altitude)<br>(Display of horizontal distance)<br>(Display of time until dropping of object) | [5] [2] [ENTER] | θ=<br>52<br>H= 19.80105063<br>L= 61.88110499<br>T= 4.020463029 |
| **5** (Display of graph of parabola) | [ENTER] |  |
| **6** | [ENTER] | H= 19.80105063<br>L= 61.88110499<br>T= 4.020463029<br>Input TX<br>Z=? |
| **7** Enter the value of time period Z.<br>(Display of distance after Z seconds)<br>(Display of altitude after Z seconds) | [3] [ENTER] | 4.020463029<br>Input TX<br>Z=<br>3<br>X= 46.17461065<br>Y= 15.00080652 |
| **8** (Altitude and distance after Z seconds are displayed on the parabola graph.) | [ENTER] |  |



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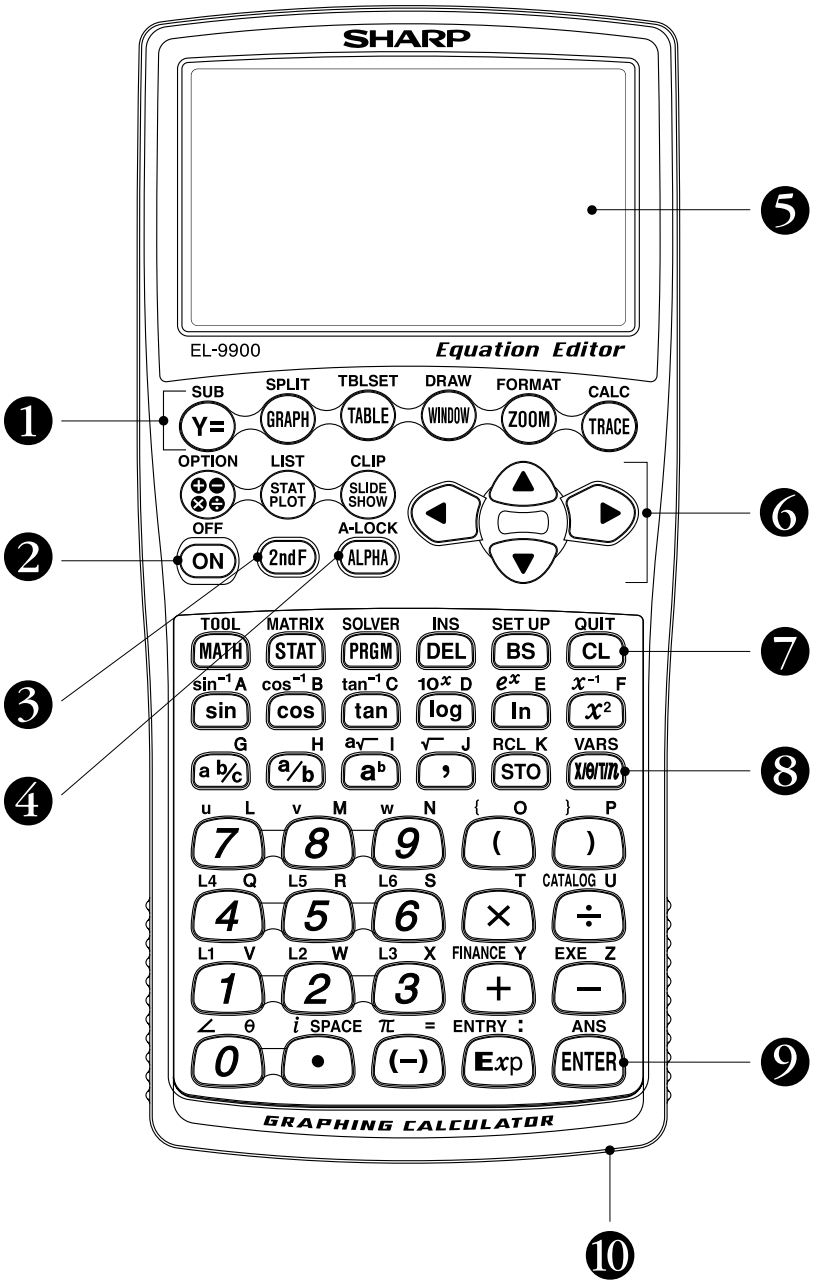
# Key pad for the SHARP EL-9900 Calculator

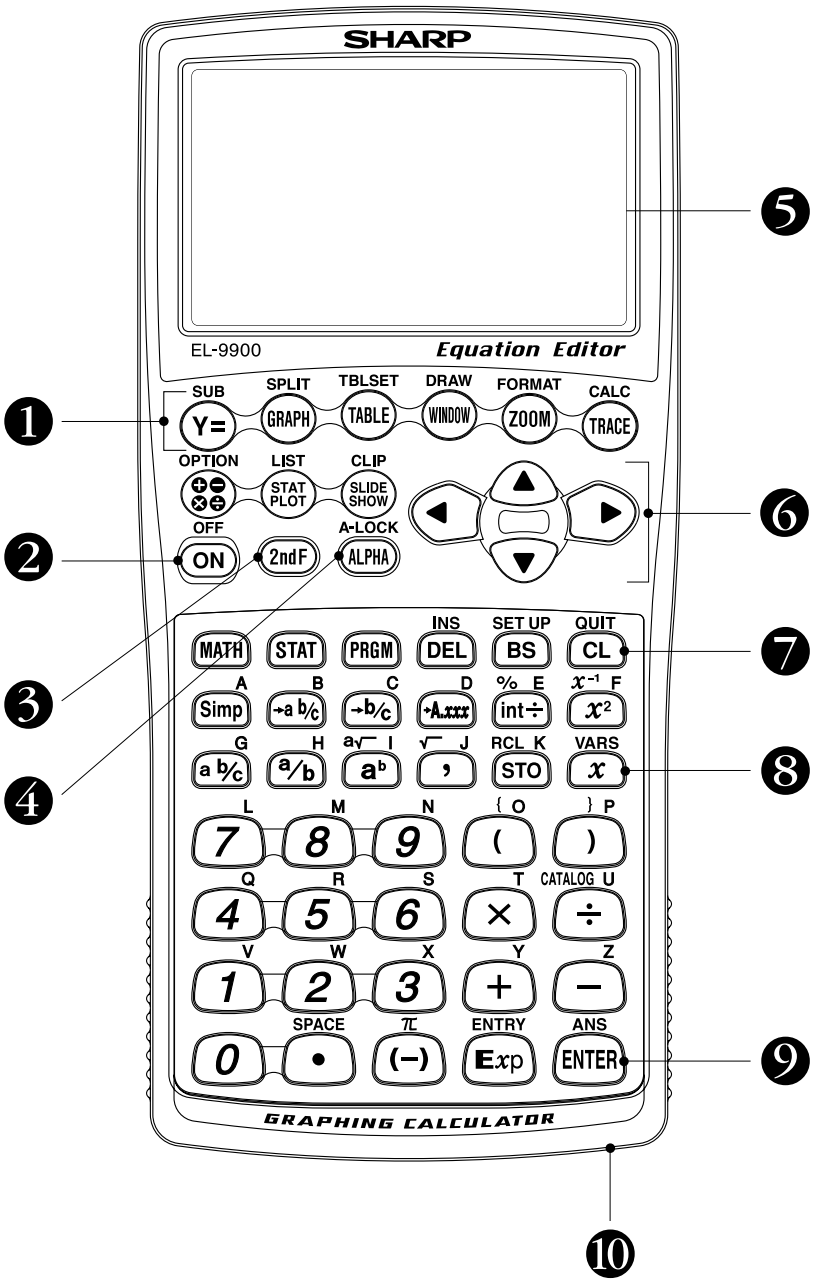
Advanced Keyboard




1. Graphing keys
2. Power supply ON/OFF key
3. Secondary function specification key
4. Alphabet specification key
5. Display screen
6. Cursor movement keys
7. Clear/Quit key
8. Variable enter key
9. Calculation execute key
10. Communication port for peripheral devices

# Key pad for the SHARP EL-9900 Calculator

Basic Keyboard




1. Graphing keys
2. Power supply ON/OFF key
3. Secondary function specification key
4. Alphabet specification key
5. Display screen
6. Cursor movement keys
7. Clear/Quit key
8. Variable enter key
9. Calculation execute key
10. Communication port for peripheral devices

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*Use this form to send us your contribution*

Dear Sir/Madam

We would like to take this opportunity to invite you to create a mathematical problem which can be solved with the SHARP EL-9900 graphing calculator, including the necessary procedures and definitions as outlined in the form below.

For this purpose, we would be grateful if you could complete the form and return it to us by fax or mail. If your contribution is chosen, your name will be included in the next edition of The EL-9900 Graphing Calculator Handbook or on our homepage. We regret that we are unable to return contributions. Also, please note that the problems you send us might be opened to the public at Sharp's home page.

We thank you for your cooperation in this project.

Name: (☐ Mr. ☐ Ms.) _____

School/College/Univ.: _____

Address: _____

_____ Post Code: _____ Country: _____

Phone: _____ Fax: _____

E-mail: _____

**SUBJECT:** Write either a title or about the subject matter.

. . . . . .

**INTRODUCTION and CALCULATION:**
Write a brief explanation of the subject, and the formula with definitions, including a diagram if relevant.

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## PARAMETERS:

Define the parameters used in the programme.

## PROGRAMME LIST:

List the procedure of data to be entered.

## EXERCISE and SET UP CONDITION:

Include an example of a problem which can be solved with the formula. Write a step-by-step guide to solving the problem with an explanation. Detail any important conditions to be set up before solving the problem.

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